## Notes—Chapter 6 Part II—Hess's Law and Enthalpies of formation

### Hess's Law

(If you have your textbooks at home, you can read through pages 260-264.)

Definition:

"When going from a particular set of reactants to a particular set of products, the change in the enthalpy ( $\Delta$ H) of the reaction is the same whether

the reaction takes place in one step or in several steps."

OR

"When a reaction takes place in more than one step, the  $\Delta H$  for the reaction is equal to the **sum** of the changes in enthalpy ( $\Delta H$ 's) of the steps."

#### **Example** (Easy example)

**Note:** I will not be putting in the "phases" of the reactants or products unless more than one phase of the same element or compound appears in the steps.

Also, the "overall reaction" refers to the reaction that would be the sum of the steps (the reaction that results from the steps).

Overall Rxn:	$N_2 + 2 O_2 \rightarrow 2$	2 NO <sub>2</sub>	ΔH = ?
Steps:	$N_2 + O_2 \rightarrow \frac{2}{2} + O_2 \rightarrow \frac{2}{2}$	2 NO 2 NO <sub>2</sub>	ΔH = +180 kJ ΔH = -112 kJ
Sum:	$N_2 + 2O_2 \rightarrow 2$	2 NO <sub>2</sub>	ΔH = +68 kJ

The sum of the equation equals the Overall Rxn. Note that the NO on opposite sides of the reactions are identical in form and amount

so they cancel through the laws of "algebra".

The  $\Delta H$  of the overall reaction is therefore, +68 kJ.

**Note:** This was an "easy example". Sometimes we must "manipulate" the steps to have them "add" up to the **overall reaction**.

If I **reverse** a reaction step (flip it). The  $\Delta H$  for that step changes its sign. Example: 2 NO  $\rightarrow$  N<sub>2</sub> + O<sub>2</sub>  $\Delta H$  = -180 kJ

(flipped)  $N_2 + O_2 \rightarrow 2 \text{ NO}$   $\Delta H = +180 \text{ kJ}$ 

If you need to **multiply or divide** a step by a number, the  $\Delta H$  of that step needs to also be multiplied or divided by that number.

Example:  $N_2 + O_2 \rightarrow 2 \text{ NO}$   $\Delta H = +180 \text{ kJ}$ 

(x2)  $2 N_2 + 2O_2 \rightarrow 4 NO$   $\Delta H = (2)(180) = +360 kJ$ Or

(÷2) ½ N <sub>2</sub> +	+ $\frac{1}{2}$ O <sub>2</sub> → NO ΔH = (180÷2) = +90 k	J
Example Probl	lem:	
Overall Reaction	on: $C_{graphite} \rightarrow C_{diamond}$	$\Delta H = ?$
Steps:		ΔН (Кј)
	a) $C_{graphite} + O_2 \rightarrow CO_2$	-394
	b) $C_{\text{diamond}} + O_2 - \rightarrow -CO_2$	<del>-396</del>
(flip step b)	$CO_2 \rightarrow C_{diamond} + O_2$	+396 (changed sign)
Now		ΔН (Кј)
	a) $C_{\text{graphite}} + -Q_2 \rightarrow CO_2$	-394
	b) $CO_{2^{-}} \rightarrow C_{diamond} + -O_{2^{-}}$	+396
Sum:	C <sub>graphite</sub> → C <sub>diamond</sub>	ΔH = +2 Kj

### Steps to follow to calculate $\Delta H$ of a reaction using Hess's Law:

- Make sure each <u>reactant</u> and each <u>product</u> in the Overall Reaction is on the <u>correct</u> side of the equation in the <u>steps</u>, flipping steps if necessary (as was done in the above example). If a reactant or a product in the overall reaction appears in more than one step, SKIP IT. It will take care of itself.
- 2) Make sure the coefficients of each reactant and product in the Overall Reaction is the same as the coefficients in the steps (multiply or divide by whatever number is necessary to make the coefficients the same making sure to include the ΔH when you do this.) If a reactant or a product in the overall reaction appears in more than one step, SKIP IT. It will take care of itself.
- 3) Cancel what is exactly the same in any step on the left with any step on the right (as done in the example above). All reactants and products in the steps must cancel if they do not appear in the overall reaction. Now add the reactants and products of the steps to show that the sum of the steps add up to the overall reaction. Add the ΔH's of the steps to obtain the ΔH of the reaction.

A more difficult example will follow on the next page.

You have problems assigned #72 and #74.

If you think you need to practice more problems, #73 and #75 are other problems to practice with the answers in the back of the book (if you have your book).

Example:

	Overall Reaction: 2	B + 3	$3 H_2 \rightarrow B_2 H_6$	ΔH = ?
			ΔΗ (k J)	
a)	$2 B + 3/2 O_2 \rightarrow B_2 H_3$		-1273	
b)	$B_2O_6 + 3O_2 \rightarrow B_2O_3 + 3H_2O_3$	)(g)	-2035	
c)	$H_2 + \frac{1}{2}O_2 \rightarrow H_2O(I)$		-286	
d)	$H_2O(I) \rightarrow H_2O(g)$		+44	
	a) b) c) d)	Overall Reaction: 2 a) $2 B + 3/2 O_2 \rightarrow B_2 H_3$ b) $B_2 O_6 + 3 O_2 \rightarrow B_2 O_3 + 3 H_2 O_2$ c) $H_2 + \frac{1}{2} O_2 \rightarrow H_2 O(1)$ d) $H_2 O(1) \rightarrow H_2 O(g)$	Overall Reaction: $2B + 3$ a) $2B + 3/2O_2 \rightarrow B_2H_3$ b) $B_2O_6 + 3O_2 \rightarrow B_2O_3 + 3H_2O(g)$ c) $H_2 + \frac{1}{2}O_2 \rightarrow H_2O(I)$ d) $H_2O(I) \rightarrow H_2O(g)$	Overall Reaction: $2 B + 3 H_2 \rightarrow B_2 H_6$ $\Delta H (k J)$ a) $2 B + 3/2 O_2 \rightarrow B_2 H_3$ -1273b) $B_2 O_6 + 3 O_2 \rightarrow B_2 O_3 + 3 H_2 O(g)$ -2035c) $H_2 + \frac{1}{2} O_2 \rightarrow H_2 O(l)$ -286d) $H_2 O(l) \rightarrow H_2 O(g)$

Note: (Each of the reactants and products in the overall reaction appear in only one of the steps so none of them can be skipped in the 3 steps we need to follow.)

Step 1:

The **reactants** in the **overall reaction** are B and H<sub>2</sub>. Check that they are on the correct side in the steps.

Both B (found in step "a") and  $H_2$  (found in step "c") are on the reactants (correct) side in the steps. **Good.** 

The **Product**,  $B_2O_6$  in step "b", is on the reactants (wrong side) and the step needs to be "flipped".

It becomes  $B_2O_3 + 3 H_2O(g) \rightarrow B_2O_6 + 3 O_2 \quad \Delta H = +2035$  (sign changes)

Steps:			ΔH (k J)
	a)	$2 B + 3/2 O_2 \rightarrow B_2 H_3$	-1273
	b)	$B_2O_3 + 3 H_2O(g) \rightarrow B_2O_6 + 3 O_2$	+2035
	c)	$H_2 + \frac{1}{2}O_2 \rightarrow H_2O(I)$	-286
	d)	$H_2O(I) \rightarrow H_2O(g)$	+44

Step 2:

Check the **coefficients** of the **reactants** and **product**s in the **overall reaction** with their coefficients in the steps.

The coefficient for B in the overall reaction is 2. The coefficient for B in step "a" is also 2. **Good** The coefficient for  $H_2$  in the reaction is 3, but the coefficient for  $H_2$  in step "c" is 1. (We must multiply through **step c** 

by 3 including the  $\Delta H$  for that step.

It becomes  $3 H_2 + 3/2 O_2 \rightarrow 3 H_2O(I)$ 

ΔH = (3)(-286) = -858 kJ

The coefficient for  $B_2O6$  is 1 and the coefficient in step "b" is 1. Good

Steps:		ΔΗ (k J)
a)	$2 B + 3/2 O_2 \rightarrow B_2 H_3$	-1273
b)	$B_2O_3 + 3 H_2O(g) \rightarrow B_2O_6 + 3 O_2$	+2035
c)	$3 H_2 + 3/2 O_2 \rightarrow 3 H_2O(I)$	-858
d)	$H_2O(I) \rightarrow H_2O(g)$	+44

Step 3:

**Cancel** All Substances that are EXACTLY the same on opposite sides of the steps.

Steps: a) $2 B + \frac{3}{2} O_2 \rightarrow B_2 H_3$ b) $B_2 O_3 + 3 H_2 O(g) \rightarrow B_2 O_6 + \frac{3}{2} O_2$ c) $3 H_2 + \frac{3}{2} O_2 \rightarrow 3 H_2 O(I)$ d) $H_2 O(I) \rightarrow H_2 O(g)$	$\Delta H (k J)$ -1273 +2035 $(3/2 O_2 + 3/2 O_2 = 3 O_2)$ -858 +44
Problem—The H <sub>2</sub> O(I) and the H <sub>2</sub> O(g) do not cance I need to multiply step "d" by 3 so all the H <sub>2</sub> O's ca "d" becomes $3 H_2O(I) \rightarrow 3 H_2O(g)$ $\Delta H = +132$	l. ncel. kJ
I now have the following:	
Steps:	ΔΗ (k J)
a) 2 B + <del>3/2 O₂ → B₂H₃</del>	-1273
b) $B_2O_3-+$ $3H_2O(g)$ $\rightarrow$ $B_2O_6$ + $3O_2$ .	+2035
c) $3 H_2 + \frac{3}{2} O_2 \rightarrow 3 H_2 O(1)$	-858
d) <del>3 H₂O(I) → 3 H₂O(g)</del>	+132
Sum: $2B + 3H_2 \rightarrow B_2O_6$	+36 kJ

Note:

This example is a lengthy on. Most Hess Law problems only have 3 steps, but it is good to practice with a more lengthy problem.

#### **Enthalpies of Formation**

In any chemical reaction, the bonds in the reactants are broken and new bonds in the products are formed.

Every compound has an Enthalpy of Formation—The amount of energy needed to form one mole of a substance

# from its elements in their standard states.

Elements in their standard or natural states have an enthalpy of formation of zero (0) kJ/mol. The Enthalpies of formation ( $\Delta H_f$ ) for elements and compounds are listed in the appendix in the back of your book.

I will send you a picture of that appendix.

You can also google them but you must make sure you have the correct "state".

You only have one problem over this for homework.

If you want to find the Enthalpy of a Reaction ( $\Delta H_{rxn}$ ), you need to add all the enthalpies of formation of the products

multiplied by their coefficients (#moles)and subtract the sum of all the enthalpies of formation of the reactants

multiplied by their coefficients (#moles). Because, when a reaction takes place,

the reactants break apart (un-form) and the products come together (form).

By subtracting the sum of the reactants, we are changing the signs of the enthalpies of formation because we are reversing the process.

The formula for finding the Enthalpy of a Reaction ( $\Delta H_{rxn}$ ) is

The sum of (add) the enthalpies of formation of the Products ( $\Delta H_{prod}$ ) times their coefficients

**minus** The sum of (add) the enthalpies of formation of the reactants ( $\Delta H_f$ ) times their coefficients.

It is written:  $\Delta H_{rxn} = \sum n (\Delta H_f)_{products} - \sum n (\Delta H_f)_{reactants}$ 

"∑" means "the sum of" so it means to add. The change in enthalpy of formations are in the back of the book.

"n" means #moles. You need to multiply the coefficients of the

Products and Reactants by their enthalpies before adding.

When you use the appendix I will post, you are looking to use the  $\Delta H^{0}_{f}$  values.(Not the  $\Delta G$  or S values)

Example:

 $2 \ C_8 H_{18} \left( I \right) \ + \ 25 \ O_2 \left( g \right) \ \rightarrow \ 16 \ CO_2 \left( g \right) \ + \ 18 \ H_2 O \left( I \right)$ 

 $\Delta H_f$  of  $C_8 H_{18}$  = -269 kJ  $\Delta H_f$  of  $O_2$  = 0  $\Delta H_f$  of  $CO_2$  = -394 kJ  $\Delta H_f$  of  $H_2O$  = -286 kJ